

Chi Square Problems With Solutions

Chi Square Problems With Solutions

Downloaded from turn-nyc-edge-vdmdp.louper.io by Wiley & Siena

UNDERSTANDING CHI SQUARE PROBLEMS WITH SOLUTIONS: A PRACTICAL GUIDE

Statistics can often feel like a maze of formulas and assumptions, but the chi-square test stands out as one of the most intuitive and widely used tools for analyzing categorical data. Whether you are a student facing an exam, a researcher testing hypotheses, or a data analyst exploring survey results, encountering **chi square problems with solutions** is inevitable. This article will demystify the chi-square test, walk you through its various applications, and present clear, step-by-step examples so you can confidently tackle any chi-square problem that comes your way.

The chi-square (χ^2) test is a non-parametric statistical method used to determine whether there is a significant association between categorical variables or whether a sample distribution matches an expected distribution. By the end of this guide, you will be able to identify which chi-square test to use, how to set up the hypotheses, calculate the test statistic, and interpret the results. Let's dive into the world of **chi square problems with solutions** and transform a challenging topic into a manageable skill.

What Is the Chi-Square Test?

The chi-square test compares observed frequencies (what you actually collect) with expected frequencies (what you would expect if there were no relationship or pattern). The core formula is:

$$\chi^2 = \sum (O - E)^2 / E$$

where O = observed count, E = expected count, and the summation is over all categories or cells. A large chi-square value indicates a large deviation from expectations, often leading to rejection of the null hypothesis.

There are three common types of chi-square tests:

- **Chi-Square Goodness-of-Fit Test** - tests if a sample distribution matches a hypothesized distribution (e.g., equal proportions).
- **Chi-Square Test of Independence** - examines whether two categorical variables are independent (e.g., gender and voting preference).
- **Chi-Square Test of Homogeneity** - checks whether different populations have the same distribution of a categorical variable (e.g., treatment outcomes across different hospitals).

Each type has its own data layout and degrees of freedom calculation, but the underlying logic remains the same. Now, let's explore concrete **chi square problems with solutions** for each type.

CHI-SQUARE GOODNESS-OF-FIT PROBLEM WITH SOLUTION

Problem 1: Do customers prefer one flavor equally?

A ice cream shop claims that customers have no preference among four flavors: vanilla, chocolate, strawberry, and mint. Over a weekend, they sell 40 vanilla, 25 chocolate, 20 strawberry, and 15 mint. Test at a significance level of $\alpha = 0.05$ whether the sales are equally distributed.

STEP 1: STATE THE HYPOTHESES

- **Null hypothesis (H_0):** Customers prefer all flavors equally (each flavor has 25% of sales).
- **Alternative hypothesis (H_1):** At least one flavor preference is different from the expected proportion.

STEP 2: CALCULATE EXPECTED FREQUENCIES

Total sales = 40 + 25 + 20 + 15 = 100. Under H_0 , each flavor expected = 100 / 4 = 25.

STEP 3: COMPUTE CHI-SQUARE STATISTIC

$$\chi^2 = \sum (O - E)^2 / E$$

- Vanilla: $(40 - 25)^2 / 25 = 225 / 25 = 9.0$
- Chocolate: $(25 - 25)^2 / 25 = 0 / 25 = 0.0$
- Strawberry: $(20 - 25)^2 / 25 = 25 / 25 = 1.0$
- Mint: $(15 - 25)^2 / 25 = 100 / 25 = 4.0$

$$\chi^2 = 9.0 + 0.0 + 1.0 + 4.0 = 14.0$$

STEP 4: DETERMINE DEGREES OF FREEDOM AND CRITICAL VALUE

df = (number of categories - 1) = 4 - 1 = 3. At $\alpha = 0.05$, the critical value from chi-square distribution table is 7.815.

STEP 5: DECISION AND INTERPRETATION

Since $\chi^2 = 14.0 > 7.815$, we reject H_0 . There is sufficient evidence that customer preferences are not equally distributed. This is a classic example of **chi square problems with solutions** involving a single categorical variable

STEP 5: DEGREES OF FREEDOM AND CRITICAL VALUE

$df = (rows - 1) \times$